

# SPLITTINGS OF d<sup>n</sup>-CONFIGURATIONS IN PENTAGONAL AND HEXAGONAL LIGAND FIELDS. COMMENTS ON THE MAGNETIC PROPERTIES AND ABSORPTION SPECTRA OF SANDWICH MOLECULES

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Most of the workers who studied the electronic structure of the sandwich molecules<sup>1-6</sup> used the covalent model as a starting point whilst few of them<sup>7-9</sup> used the ionic model. We have tried to get to some qualitative conclusions concerning the magnetic properties and spectral behaviour of di- $\pi$ -cyclopentadiene and dibenzene compounds of transition metals, on the basis of the purely ionic model assuming ligand fields of  $D_{5d}$  or  $D_{5h}$  and  $D_{6h}$  symmetries.

First we assume that the central ion in the sandwich molecules consists of a point-like ionic core and one d-electron, and the five- and six-membered rings are regular pentagons (C-C bond distance is 1.46 Å) and hexagons (C-C bond distance is 1.39 Å) in which the apices represent ligands of an effective point charge  $Z > 0$ . It was in these systems that the energies of the single d-electron have been calculated. The electron has an energy in the field of the free central ion to which contributes the effect of the ligands represented by a potential:

$$V_s = - \sum_j \frac{Z \cdot e^2}{|\vec{R}_j - \vec{r}|} \quad (1)$$

where  $\vec{R}_j$  is the position vector of the  $j$ -th ligand and  $\vec{r}$  that of the d-electron. The energy contributions are then given by integrals of the type

$$\langle \psi | V_s | \psi \rangle$$

where  $\psi$  is a linear combination of the five d-orbitals. Disregarding the factor  $-Z \cdot e^2$  the forms of  $V_s$  in  $D_{5d}$  or  $D_{5h}$  and in  $D_{6h}$  are

$$V_5 = 10 \frac{r_0^0}{r_1^2} + 10 \frac{r_2^2}{r_3^2} P_2(\cos \vartheta_0) P_2(\cos \vartheta) + 10 \frac{r_4^4}{r_5^2} P_4^{(1)}(\cos \vartheta_0) P_4(\cos \vartheta) \quad (2a)$$

and

$$V_6 = 12 \frac{r_0^0}{r_1^2} + 12 \frac{r_2^2}{r_3^2} P_2(\cos \vartheta_0) P_2(\cos \vartheta) + 12 \frac{r_4^4}{r_5^2} P_4(\cos \vartheta_0) P_4(\cos \vartheta) \quad (2b)$$

and the corresponding one-electron integrals

$$\langle \pm 2 | V_5 | \pm 2 \rangle = \frac{80}{45} f G(0) - \frac{160}{315} f G(2) P_2(\cos \vartheta_0) + \frac{80}{945} f G(4) P_4(\cos \vartheta_0) \quad (3a)$$

$$\langle \pm 1 | V_5 | \pm 1 \rangle = \frac{80}{45} f G(0) + \frac{80}{315} f G(2) P_2(\cos \vartheta_0) - \frac{320}{945} f G(4) P_4(\cos \vartheta_0) \quad (3b)$$

$$\langle 0 | V_5 | 0 \rangle = \frac{80}{45} f G(0) + \frac{160}{315} f G(2) P_2(\cos \vartheta_0) + \frac{480}{945} f G(4) P_4(\cos \vartheta_0) \quad (3c)$$

and

$$\langle \pm 2 | V_6 | \pm 2 \rangle = \frac{96}{45} f G(0) - \frac{192}{315} f G(2) P_2(\cos \vartheta_0) + \frac{96}{945} f G(4) P_4(\cos \vartheta_0) \quad (4a)$$

$$\langle \pm 1 | V_6 | \pm 1 \rangle = \frac{96}{45} f G(0) + \frac{96}{315} f G(2) P_2(\cos \vartheta_0) - \frac{384}{945} f G(4) P_4(\cos \vartheta_0) \quad (4b)$$

$$\langle 0 | V_6 | 0 \rangle = \frac{96}{45} f G(0) + \frac{192}{315} f G(2) P_2(\cos \vartheta_0) + \frac{576}{945} f G(4) P_4(\cos \vartheta_0) \quad (4c)$$

in which

$$f = \frac{Z_c}{3 \cdot a_0}, \quad (5)$$

$Z_c$  is the effective charge of the central ion,  $\vartheta_0$  the polar angle of the ligands determined at a given  $R$  by the sizes of the cyclopentadiene or benzene rings (Fig. 1), and

$$G(n) = \int_0^R (fr)^6 \frac{r^n}{R^{n+1}} e^{-2fr} dr + \int_R^\infty (fr)^6 \frac{R^n}{r^{n+1}} e^{-2fr} dr \quad (6)$$

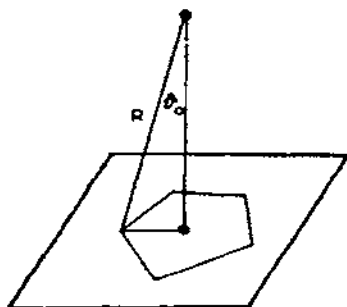


Fig. 1.

where  $r$  is the distance between the electron and the central ion and  $R$  that between the ligand and the central ion, and  $n = 0, 2$  or  $4$ .

Introducing the following notations

$$D_0(5) = \frac{80}{45} fG(0) \quad (7a)$$

$$D_2(5) = \frac{80}{315} fG(2)P_2(\cos \vartheta_0) \quad (7b)$$

$$D_4(5) = \frac{80}{945} fG(4)P_4(\cos \vartheta_0) \quad (7c)$$

and

$$D_0(6) = \frac{96}{45} fG(0) \quad (8a)$$

$$D_2(6) = \frac{96}{315} fG(2)P_2(\cos \vartheta_0) \quad (8b)$$

$$D_4(6) = \frac{96}{945} fG(4)P_4(\cos \vartheta_0) \quad (8c)$$

respectively, we get formally the same expressions for both symmetries:

$$\langle 2 | V_a | 2 \rangle = D_0(s) - 2D_2(s) + D_4(s), \quad (9a)$$

$$\langle 1 | V_a | 1 \rangle = D_0(s) + D_2(s) - 4D_4(s), \quad (9b)$$

$$\langle 0 | V_a | 0 \rangle = D_0(s) + 2D_2(s) + 6D_4(s). \quad (9c)$$

This result, of course, agrees with that of other authors<sup>10-12</sup> who investigated problems of axial symmetries.

Since in  $D_3$  or  $D_6$  symmetries\* the d-orbitals split in the form:

$$\Gamma = A_1 + E_1 + E_2 \quad (10)$$

and since

$d_0$  transforms like  $A_1$

$d_{\pm 1}$  like  $E_1$  and

$d_{\pm 2}$  like  $E_2$

the expressions (9a, 9b, 9c) actually give the energies belonging to the corresponding irreducible representations.

The numerical evaluation of the one-electron energies does not cause much trouble. By using the substitution

$$a = f \cdot R$$

\* For simplicity we deal with  $D_3$  and  $D_6$  symmetries instead of  $D_{3d}$  or  $D_{6h}$  and  $D_{4h}$  symmetries.

we get for  $G(n)$  that

$$G(n) = a^6 \left\{ \frac{(n+6)!}{(2a)^{n+7}} - A_{n+6}(2a) + A_{5-n}(2a) \right\} \quad (11)$$

where

$$A_m(\alpha) = \int_1^\infty e^{-\alpha x} \cdot x^m dx \quad (12)$$

For the probable values of  $f$  and  $R$  ( $f = 1-3$  au and  $R = 4-6$  au\*) we calculated the one-electron energies and found that, as a rule, the sequence of the energies—regarding the minus sign in the factor  $-Z \cdot e^2$ —is

$$a_1 < e_1 < e_2$$

In the Tables 1 and 2 the energy differences  $\Delta_1$  ( $= E(a_1) - E(e_1)$ ) and  $\Delta_2$  ( $= E(e_1) - E(e_2)$ ) are given. It can be seen from the Tables that, in general,  $\Delta_1$  and  $\Delta_2$  are of the same order of magnitude and the larger is  $R$  or  $Z_c(f)$  the smaller is the difference between them.

TABLE 1

$D_3$	$f$			
$R$	1	2	3	
4	$\Delta_2$	0.3221	0.1215	0.0527
	$\Delta_1$	0.0047	0.0195	0.0129
5	$\Delta_2$	0.2489	0.0789	0.0346
	$\Delta_1$	0.1168	0.0298	0.0127
6	$\Delta_2$	0.1742	0.0520	0.0232
	$\Delta_1$	0.1164	0.0220	0.0089

TABLE 2

$D_4$	$f$			
$R$	1	2	3	
4	$\Delta_2$	0.3323	0.1164	0.0479
	$\Delta_1$	-0.0969	-0.0032	0.0078
5	$\Delta_2$	0.2841	0.0856	0.0370
	$\Delta_1$	0.0772	0.0262	0.0120
6	$\Delta_2$	0.2025	0.0585	0.0268
	$\Delta_1$	0.1095	0.0230	0.0101

It can also be pointed out that by increasing  $R$  or  $Z_c$  both the absolute values of the energies and the energy differences  $\Delta_1$  and  $\Delta_2$  are decreased.

On the basis of the above considerations two cases can be distinguished. In the first case the separations  $\Delta_1$  and  $\Delta_2$  (Fig. 2) are relatively large. By increasing  $R$  or  $Z_c$ , or both of them, the first case turns into the second one where the separations  $\Delta_1$  and  $\Delta_2$  are small.

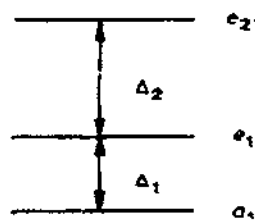


Fig. 2.

\* 1 au = 109700 cm<sup>-1</sup>

TABLE 3<sup>a</sup>

No. of electrons	Electron configuration Ion	Molecule	Ground state	Excited Configurations	States	Examples
0	$d^2$	$(a_1)^2$	$^1A_1$	$(a_1)(e_1)$ $(a_1)(e_2)$	$^1E_1$ $^1E_2$	Ti(cp) <sub>2</sub> Mo(cp) <sub>2</sub> <sup>2+</sup>
1	$d^3$	$(a_1)^2(e_1)$	$^3E_1$	$(a_1)(e_1)(e_2)$ $(a_1)(e_1)^2$ $(a_1)^2(e_2)$	$2^3E_1, 2^3E_2$ $^3A_1, ^3A_2, ^3E_2$ $^3E_2$	—
2	$d^4$	$(a_1)^2(e_1)^2$	$^3A_2$	$(a_1)(e_1)^3$ $(a_1)(e_1)^2(e_2)$ $(a_1)^2(e_1)(e_2)$	$^3E_1$ $^3A_1, ^3A_2, ^3E_1, 3^3E_2$ $^3E_1, ^3E_2$	Cr(cp) <sub>2</sub>
1	$d^5$	$(a_1)^2(e_1)^3$	$^2E_1$	$(a_1)(e_1)^4$ $(a_1)(e_1)^3(e_2)$ $(a_1)^2(e_1)^2(e_2)$	$^2A_1$ $2^2E_1, 2^2E_2$ $^2A_1, ^2A_2, ^2E_1$ $2^2E_2$	Fe(cp) <sub>2</sub> <sup>+</sup> (V(bz) <sub>2</sub> ) (Cr(bz) <sub>2</sub> ) <sup>+</sup>
0	$d^6$	$(a_1)^2(e_1)^4$	$^1A_1$	$(a_1)^2(e_1)^3(e_2)$ $(a_1)(e_1)^4(e_2)$	$^1E_1, ^1E_2$ $^1E_2$	Fe(cp) <sub>2</sub> Co(cp) <sub>2</sub> <sup>+</sup> Rh(cp) <sub>2</sub> <sup>+</sup> Ru(cp) <sub>2</sub> Ir(cp) <sub>2</sub> <sup>+</sup> (Cr(bz) <sub>2</sub> )
1	$d^7$	$(a_1)^2(e_1)^4(e_2)$	$^2E_2$	$(a_1)(e_1)^4(e_2)^2$ $(a_1)^2(e_1)^3(e_2)^2$	$^2A_1, ^2A_2, ^2E_1$ $^2A_1, ^2A_2, 2^2E_1, ^2E_2$	Co(cp) <sub>2</sub> Ni(cp) <sub>2</sub> <sup>+</sup>

<sup>a</sup> The data of Tables 3 and 4 are those for  $D_3$  symmetry, therefore, they are only valid for the cyclopentadiene compounds. Minor deviations in the (excited) many-electron states occur for  $D_4$  symmetry (see Ref. 13).

In order to interpret the magnetic properties of the sandwich molecules, let us fill up one-by-one the one-electron states with electrons. It is obvious that the energy distribution related with the first case is favourable to the so called "low spin case" and the second, to the "high spin case". The electron configurations corresponding to these cases are given in the third columns of the Tables 3 and 4. As it can be seen, for a number of cyclopentadiene and for a few benzene compounds (last columns) the numbers of unpaired electrons (first columns) agree with those corresponding to the electron configurations in the normal states. If one found that for a given case the calculated and observed energy distribution or electron configuration were different, it would mean (i) that the presented ionic model could not be applied to that particular case, or (ii) that the sandwich rings suffered distortion and as a consequence one should have different  $\vartheta_2$  polar angles at a given constant  $R$ .

To be able to explain, at least qualitatively, the spectral behaviour of these molecules, the many-electron states arising from the splittings, in fields of  $D_3$  and  $D_6$  symmetries, of electron configurations<sup>1,3</sup> have to be considered. The fourth columns of Tables 3 and 4 show the ground states corresponding to the electron

TABLE 4

No. of electrons	Electron configuration		Ground state	Excited		Examples
	ion	Molecule		Configurations	States	
2	d <sup>2</sup>	(a <sub>1</sub> ) (e <sub>1</sub> )	<sup>3</sup> E <sub>1</sub>	(e <sub>1</sub> ) <sup>3</sup> (e <sub>1</sub> ) (e <sub>2</sub> ) (a <sub>1</sub> ) (e <sub>2</sub> )	<sup>3</sup> A <sub>2</sub> <sup>3</sup> E <sub>1</sub> , <sup>3</sup> E <sub>2</sub> <sup>3</sup> E <sub>2</sub>	V(cp) <sub>2</sub> <sup>+</sup>
3	d <sup>3</sup>	(a <sub>1</sub> ) (e <sub>1</sub> ) <sup>2</sup>	<sup>4</sup> A <sub>2</sub>	(e <sub>1</sub> ) <sup>3</sup> (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> ) (a <sub>1</sub> ) (e <sub>1</sub> ) (e <sub>2</sub> )	— <sup>4</sup> E <sub>2</sub> <sup>4</sup> E <sub>1</sub> , <sup>4</sup> E <sub>2</sub>	V(cp) <sub>2</sub> Cr(cp) <sub>2</sub> <sup>+</sup>
4	d <sup>4</sup>	(a <sub>1</sub> ) (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> )	<sup>5</sup> E <sub>2</sub>	(e <sub>1</sub> ) <sup>3</sup> (e <sub>2</sub> ) (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> ) <sup>2</sup> (a <sub>1</sub> ) (e <sub>1</sub> ) (e <sub>2</sub> ) <sup>2</sup>	— <sup>5</sup> A <sub>1</sub> <sup>5</sup> E <sub>1</sub>	—
5	d <sup>5</sup>	(a <sub>1</sub> ) (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> ) <sup>2</sup>	<sup>6</sup> A <sub>1</sub>	—	—	Mn(cp) <sub>2</sub>
4	d <sup>6</sup>	(a <sub>1</sub> ) <sup>2</sup> (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> ) <sup>2</sup>	<sup>3</sup> A <sub>1</sub>	(a <sub>1</sub> ) (e <sub>1</sub> ) <sup>3</sup> (e <sub>2</sub> ) <sup>2</sup> (a <sub>1</sub> ) (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> ) <sup>3</sup> (a <sub>1</sub> ) <sup>2</sup> (e <sub>1</sub> ) (e <sub>2</sub> ) <sup>3</sup>	<sup>3</sup> E <sub>1</sub> <sup>3</sup> E <sub>2</sub> —	—
3	d <sup>7</sup>	(a <sub>1</sub> ) <sup>3</sup> (e <sub>1</sub> ) <sup>3</sup> (e <sub>2</sub> ) <sup>2</sup>	<sup>4</sup> E <sub>1</sub>	(a <sub>1</sub> ) (e <sub>1</sub> ) <sup>4</sup> (e <sub>2</sub> ) <sup>2</sup> (a <sub>1</sub> ) (e <sub>1</sub> ) <sup>3</sup> (e <sub>2</sub> ) <sup>3</sup> (a <sub>1</sub> ) <sup>3</sup> (e <sub>1</sub> ) <sup>2</sup> (e <sub>2</sub> ) <sup>3</sup>	<sup>4</sup> A <sub>2</sub> <sup>4</sup> E <sub>1</sub> , <sup>4</sup> E <sub>2</sub> <sup>4</sup> E <sub>2</sub>	—
1	d <sup>1</sup>	(a <sub>1</sub> )	<sup>2</sup> A <sub>1</sub>	(e <sub>1</sub> ) (e <sub>2</sub> )	<sup>2</sup> E <sub>1</sub> <sup>2</sup> E <sub>2</sub>	Ti(cp) <sub>2</sub> <sup>+</sup> V(cp) <sub>2</sub> <sup>2+</sup>
2	d <sup>6</sup>	(a <sub>1</sub> ) <sup>2</sup> (e <sub>1</sub> ) <sup>4</sup> (e <sub>2</sub> ) <sup>2</sup>	<sup>3</sup> A <sub>1</sub>	(a <sub>1</sub> ) (e <sub>1</sub> ) <sup>4</sup> (e <sub>2</sub> ) <sup>3</sup> (a <sub>1</sub> ) <sup>2</sup> (e <sub>1</sub> ) <sup>3</sup> (e <sub>2</sub> ) <sup>3</sup>	<sup>3</sup> E <sub>2</sub> <sup>3</sup> E <sub>1</sub> , <sup>3</sup> E <sub>2</sub>	Ni(cp) <sub>2</sub>
1	d <sup>9</sup>	(a <sub>1</sub> ) <sup>2</sup> (e <sub>1</sub> ) <sup>4</sup> (e <sub>2</sub> ) <sup>3</sup>	<sup>2</sup> E <sub>2</sub>	(a <sub>1</sub> ) <sup>3</sup> (e <sub>1</sub> ) <sup>3</sup> (e <sub>2</sub> ) <sup>4</sup> (a <sub>1</sub> ) (e <sub>1</sub> ) <sup>4</sup> (e <sub>2</sub> ) <sup>4</sup>	<sup>2</sup> E <sub>1</sub> <sup>2</sup> A <sub>1</sub>	—

configurations in the normal states as well as the excited levels (sixth columns), considering only one-electron jumps (fifth columns) from the ground electron configurations.

Finally, we would like to touch upon a few examples to compare these qualitative results with experimental data from the literature (Table 5).

TABLE 5<sup>a</sup>

Molecule	Probable d-d bands in Å		Reference (14)
Ni(cp) <sub>2</sub>	5700	4400	a
Fe(cp) <sub>2</sub>	4400	(3200)	b
Ru(cp) <sub>2</sub>	3300	2700	c
Co(cp) <sub>2</sub> <sup>+</sup>	4200	3200	d
Rh(cp) <sub>2</sub> <sup>+</sup>		3200	
Ir(cp) <sub>2</sub> <sup>+</sup>		3000	e <sup>b</sup>

<sup>a</sup> Spectral data for other compounds are rather scarce, e.g. for Cr(bz)<sub>2</sub> and Cr(bz)<sub>2</sub><sup>+</sup> see Refs. 15 and 16.

<sup>b</sup> The broad tail, in the absorption spectra, towards the longer wavelengths may cover several bands.

Theoretically, in all the cases given in Table 5 three transitions are possible (see Tables 3 and 4) and one can expect certain similarity in the absorption spectra of low spin  $d^6$  (Table 3) and  $d^8$  (Table 4) systems seeing that for both systems a non-degenerate ( $A$ ) state is the ground level and the three excited levels are doubly degenerate ( $E$ ) states. To select the true transitions from the possible ones, calculation of interelectronic repulsions should be carried out but considering that the presented model is a rather rough and simple approach to the real problem there would have been no much point in doing it.

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